

1.21 The pressure of the gas contained in the piston-cylinder assembly of Fig. 1.1 varies with its volume according to $p = A + (B/V)$, where A, B are constants. If pressure is in lbf/ft^2 and volume is in ft^3 , what are the units of A and B?

KNOWN: Relationship between pressure and volume.

FIND: Determine units of A and B.

SCHEMATIC AND GIVEN DATA:

$$p \text{ [lbf/ft}^2\text{]}$$

$$V \text{ [ft}^3\text{]}$$

$$p = A + (B/V), \text{ where A and B are constants}$$

ENGINEERING MODEL:

1. The gas is a closed system.

ANALYSIS:

$$\begin{array}{c}
 p = A + \frac{B}{V} \\
 \uparrow \qquad \swarrow \\
 \left[\frac{\text{lbf}}{\text{ft}^2} \right] \quad \left[\text{ft}^3 \right]
 \end{array}$$

By inspection of this equation, **A has units of lbf/ft^2 .**

Rearranging,

$$\begin{array}{c}
 B = \underbrace{[p - A]}_{\left[\frac{\text{lbf}}{\text{ft}^2} \right]} \underbrace{V}_{\left[\text{ft}^3 \right]}
 \end{array}$$

\Rightarrow **B has units of $\text{ft}\cdot\text{lbf}$.**